

# MBA-Blast: Unveiling and Simplifying Mixed Boolean-Arithmetic Obfuscation

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Binbin Liu, Junfu Shen, Jiang Ming, Qilong Zheng, Jing Li, Dongpeng Xu

Let us look at an MBA obfuscation example!

```

int fun(int x,int y,int z)
{
    int c;
    c = x+y;

    return c;
}

```

(a) Original program.

```

int fun(int x,int y,int z)
{
    int c;
    c = 4*(~x&y) - (x^y) - (x|y)
        +4*~(x|y) - ~(x^y) - ~y -
        (x|~y)+1+6*x+5*~z+
        (~(x^z)) - (x|z) - 2*~x -
        4*(~(x|z)) - 4*(x&~z)
        +3*(~(x|~z));

    return c;
}

```

(b) MBA obfuscated program.

Background

# MBA Expression

Mixed Boolean-Arithmetic (MBA) expression mix Boolean operators ( $|$ ,  $\&$ , ...) and arithmetic operations ( $+$ ,  $-$ ,  $*$ , ...).

**Definition 1.** An MBA expression is :

$$\sum_{i \in I} a_i e_i(x_1, \dots, x_t),$$

$a_i$  is a constant coefficient,

$e_i(x_1, \dots, x_t)$  are bitwise expressions of variables  $x_1, \dots, x_t$ .

$a_i e_i(x_1, \dots, x_t)$  is called a term in the MBA expression.

$$2 * (x | y) - (\neg x \& y) - (\sim x \& y) - 9$$
$$X + y - (x \& y) - 3 * (x \wedge y) + 5$$

# MBA Obfuscation

## *Academia:*

- Tigress: C source code obfuscator.

## *Industry:*

- Cloakware
- Irdeto
- Quarkslab

## *Malware:*

- VMProtect

# MBA Deobfuscation

## *Existing software:*

- Symbolic software: SagaMath, Wolfram Mathematica, Maple.
- SMT solver: Boolector, STP, Z3.

## *Related work:*

- Arybo: normalizes MBA expressions to bit-level symbolic expressions.
- SSPAM: simplifies MBA expression by a pattern matching algorithm.
- Syntia: use program synthesis techniques to simplify MBA expressions.

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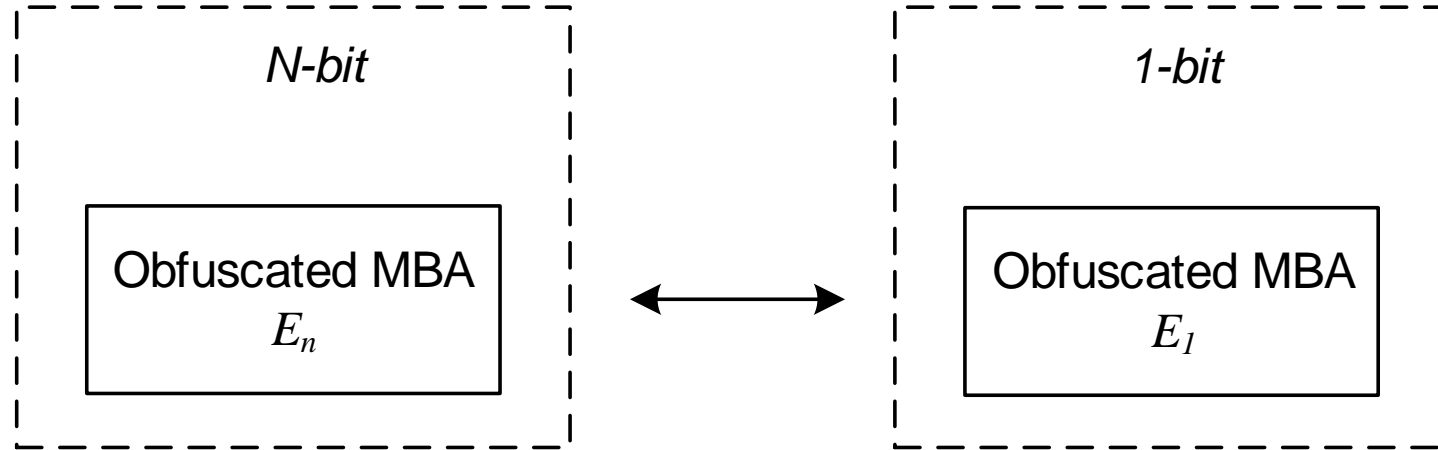
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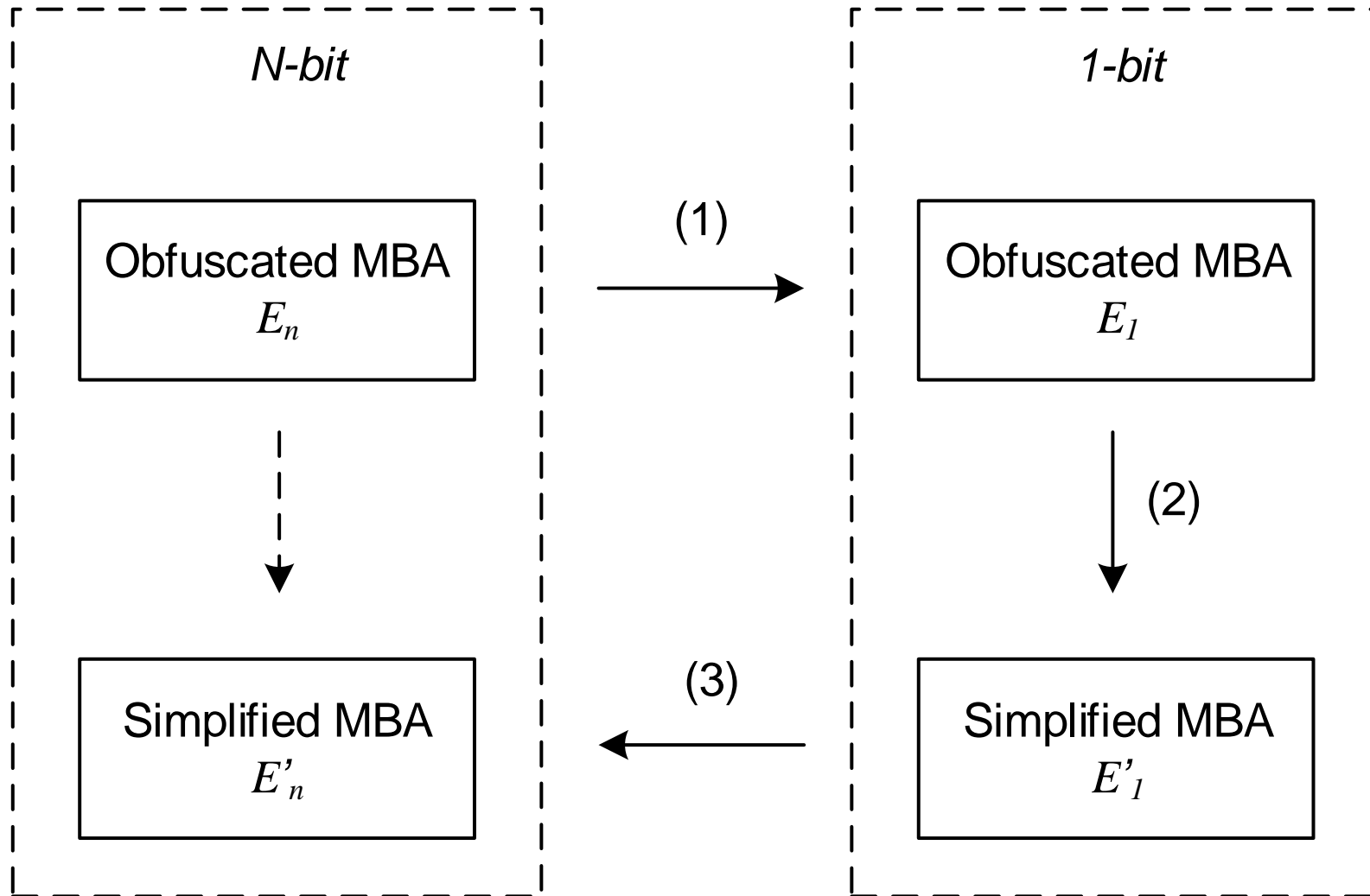


# Our Approach

# Two-way Feature



# Logic Flow of MBA-Blast Simplification



## 2-Variable Truth Table

Truth Table	Boolean Expression
$[0,0,0,0]^T$	0
$[0,0,0,1]^T$	$x \& y$
$[0,0,1,0]^T$	$x \& \sim y$
$[0,0,1,1]^T$	$x$
$[0,1,0,0]^T$	$\sim x \& y$
... ..	... ..
$[1,0,1,1]^T$	$x   \sim y$
$[1,1,0,0]^T$	$\sim x$
$[1,1,0,1]^T$	$\sim x   y$
$[1,1,1,0]^T$	$\sim(x \& y)$
$[1,1,1,1]^T$	-1

## 2-Variable Boolean Normalization

Truth Table	Boolean Expression	MBA Expression
$[0,0,0,0]^T$	0	0
$[0,0,0,1]^T$	$x \& y$	$x \& y$
$[0,0,1,0]^T$	$x \& \sim y$	$x - (x \& y)$
$[0,0,1,1]^T$	$x$	$x$
$[0,1,0,0]^T$	$\sim x \& y$	$y - (x \& y)$
... ..	... ..	... ..
$[1,0,1,1]^T$	$x   \sim y$	$-y + (x \& y) - 1$
$[1,1,0,0]^T$	$\sim x$	$-x - 1$
$[1,1,0,1]^T$	$\sim x   y$	$-x + (x \& y) - 1$
$[1,1,1,0]^T$	$\sim(x \& y)$	$-(x \& y) - 1$
$[1,1,1,1]^T$	-1	-1

$$e_i(x, y) = c_1 x + c_2 y + c_3 (x \& y) - c_4$$

# MBA Simplification

$$\begin{aligned} & \mathbf{e}_i(\mathbf{x}, \mathbf{y}) \\ &= c_1 \mathbf{x} + c_2 \mathbf{y} + c_3 (\mathbf{x} \& \mathbf{y}) - c_4 \end{aligned}$$



$$\begin{aligned} & \sum_{i \in I} a_i \mathbf{e}_i(\mathbf{x}, \mathbf{y}) \\ &= \sum_{i \in I} a_i * (c_{1i} \mathbf{x} + c_{2i} \mathbf{y} + c_{3i} (\mathbf{x} \& \mathbf{y}) - c_{4i}) \\ &= \mathbf{C}_1 \mathbf{x} + \mathbf{C}_2 \mathbf{y} + \mathbf{C}_3 (\mathbf{x} \& \mathbf{y}) - \mathbf{C}_4 \end{aligned}$$

# MBA Simplification Algorithm

MBA expression

$$2^*(x|y) - (\sim x \& y) - (x \& \sim y) - 2^*(x \& y)$$



# MBA Simplification Algorithm

MBA expression

Boolean Normalization

$$e_i(x, y) = c_1x + c_2y + c_3(x&y) - c_4$$

$$2^*(x|y) - (\sim x \& y) - (x \& \sim y) - 2^*(x \& y)$$

$$2^*(x + y - (x \& y)) - (y - (x \& y)) - (x - (x \& y)) - 2^*(x \& y)$$

# MBA Simplification Algorithm

MBA expression

Boolean Normalization

$$e_i(x, y) = c_1x + c_2y + c_3(x&y) - c_4$$

Arithmetic Reduction

$$\begin{aligned} & \sum_{i \in I} a_i e_i(x, y) \\ &= \sum_{i \in I} a_i * (c_{1i}x + c_{2i}y + c_{3i}(x&y) - c_{4i}) \\ &= C_1x + C_2y + C_3(x&y) - C_4 \end{aligned}$$

$$2^*(x|y) - (\sim x \& y) - (x \& \sim y) - 2^*(x \& y)$$

$$2^*(x + y - (x \& y)) - (y - (x \& y)) - (x - (x \& y)) - 2^*(x \& y)$$

$$\begin{aligned} & 2^*x + 2^*y - 2^*(x \& y) - y + (x \& y) - x + (x \& y) - 2^*(x \& y) \\ &= x + y - 2^*(x \& y) \end{aligned}$$

# MBA Simplification Algorithm

MBA expression

Boolean Normalization

$$e_i(x, y) = c_1x + c_2y + c_3(x&y) - c_4$$

Arithmetic Reduction

$$\begin{aligned} & \sum_{i \in I} a_i e_i(x, y) \\ &= \sum_{i \in I} a_i * (c_{1i}x + c_{2i}y + c_{3i}(x&y) - c_{4i}) \\ &= C_1x + C_2y + C_3(x&y) - C_4 \end{aligned}$$

Optimization

Simple bitwise expression?

$$2^*(x|y) - (\sim x \& y) - (x \& \sim y) - 2^*(x \& y)$$

$$2^*(x + y - (x \& y)) - (y - (x \& y)) - (x - (x \& y)) - 2^*(x \& y)$$

$$\begin{aligned} & 2^*x + 2^*y - 2^*(x \& y) - y + (x \& y) - x + (x \& y) - 2^*(x \& y) \\ &= \boxed{x + y - 2^*(x \& y)} \end{aligned}$$

$$\boxed{x \wedge y}$$

# Evaluation

# MBA Dataset

## *Setup*

- 10,000 MBA expressions
  - Length of variables
  - Number of variables
  - Number of terms
- Intel Xeon CPU and 64GB RAM
- Compared with peer tools
  - Arybo
  - SSPAM
  - Syntia
- Z3 solver for checking simplified result
  - Timeout threshold: five hours

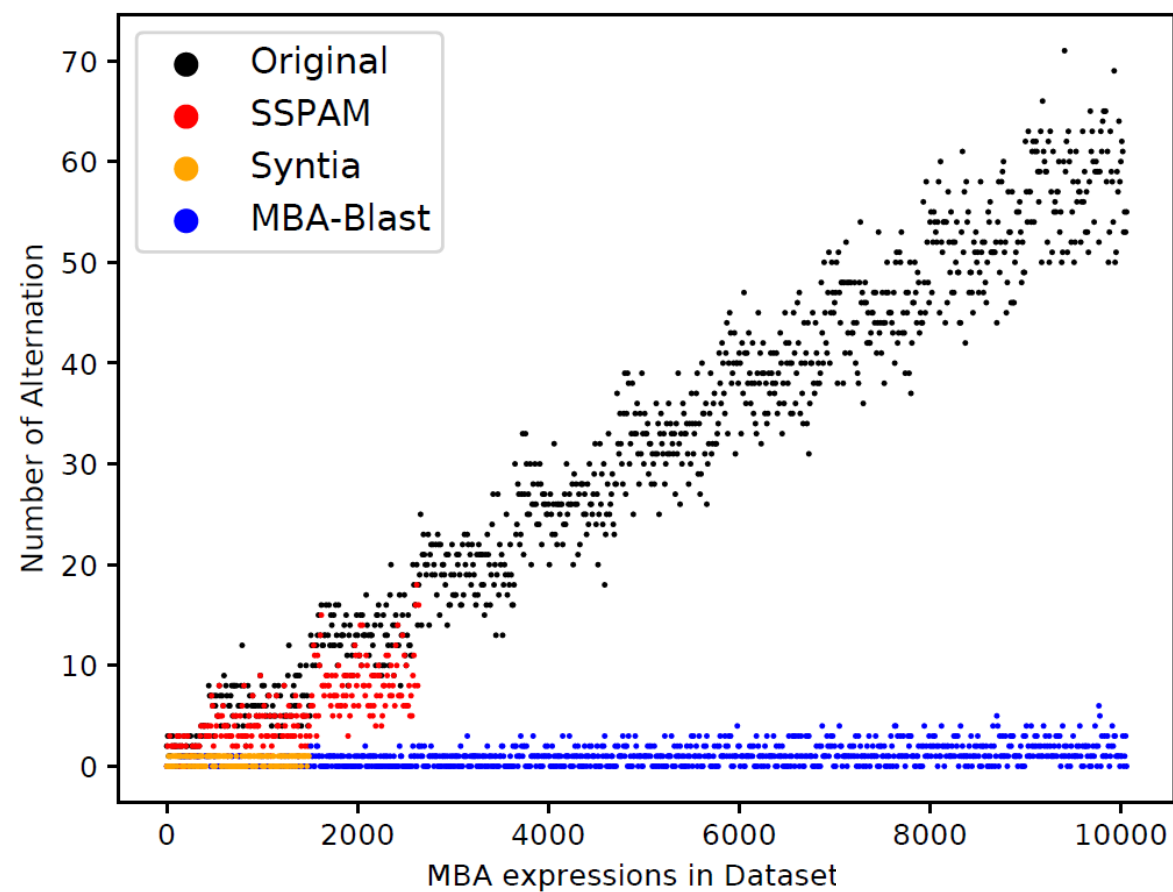
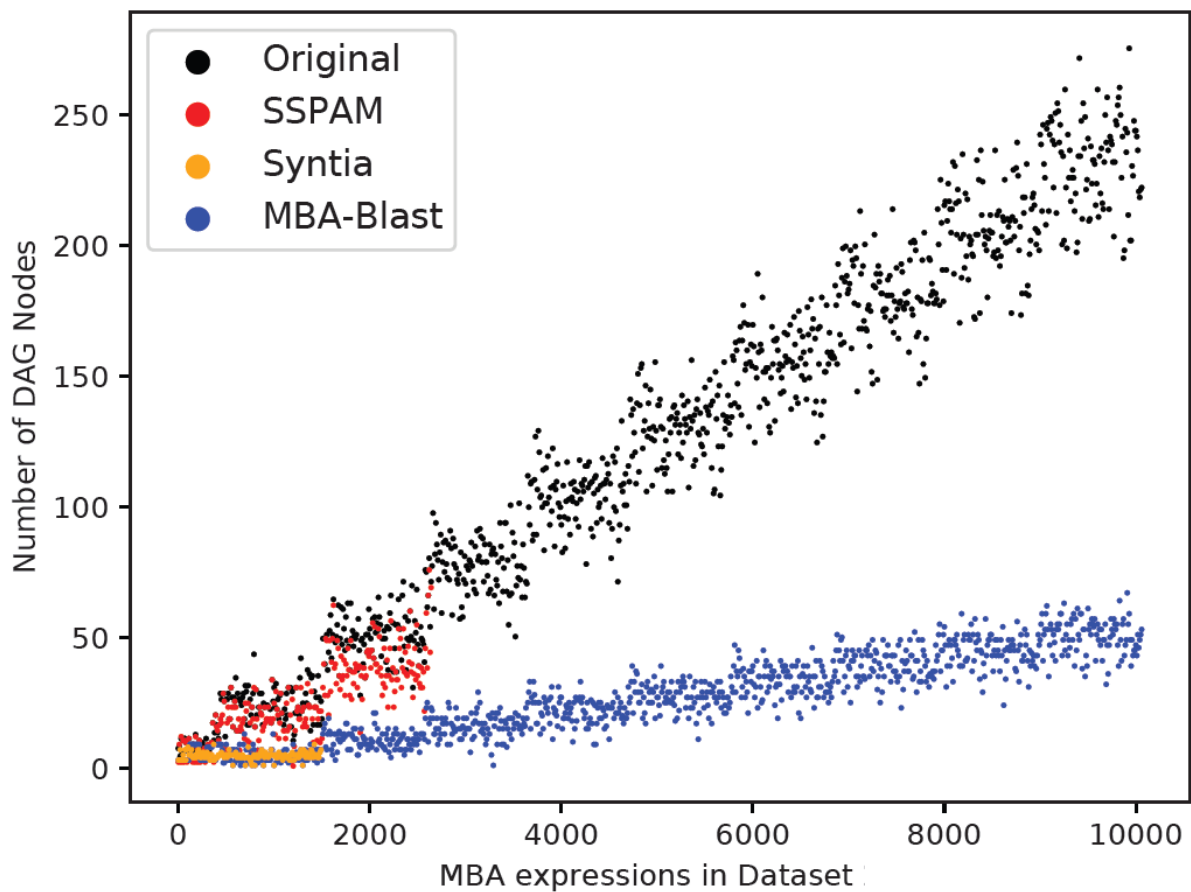
# MBA Dataset

## *Simplification Results*

Method	Simplification Results				Average Processing Time (Seconds/Sample)
	Yes	No	T.O	Ratio(%)	
Arybo	431	0	9569	4.3	640.7
SSPAM	2550	0	7450	25.5	438.2
Syntia	1438	8562	0	14.1	9.3
<b>MBA-Blast</b>	<b>10,000</b>	<b>0</b>	<b>0</b>	<b>100.0</b>	<b>0.05</b>

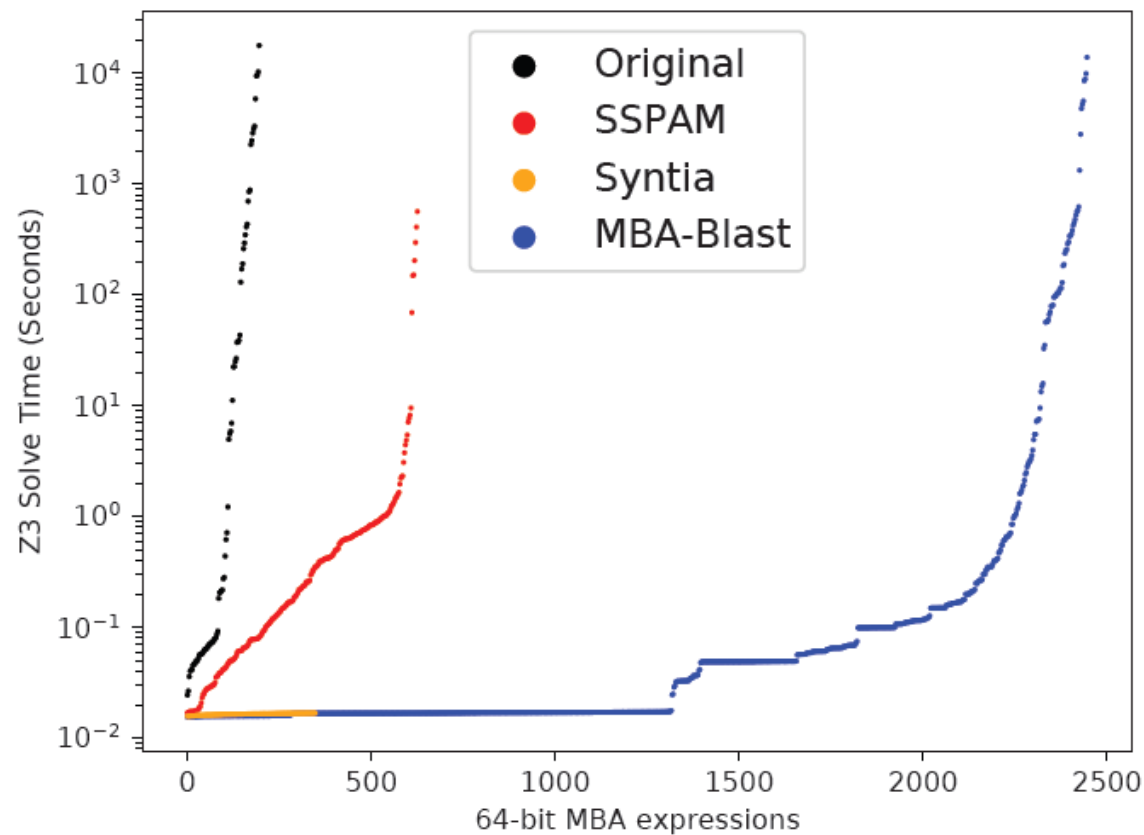
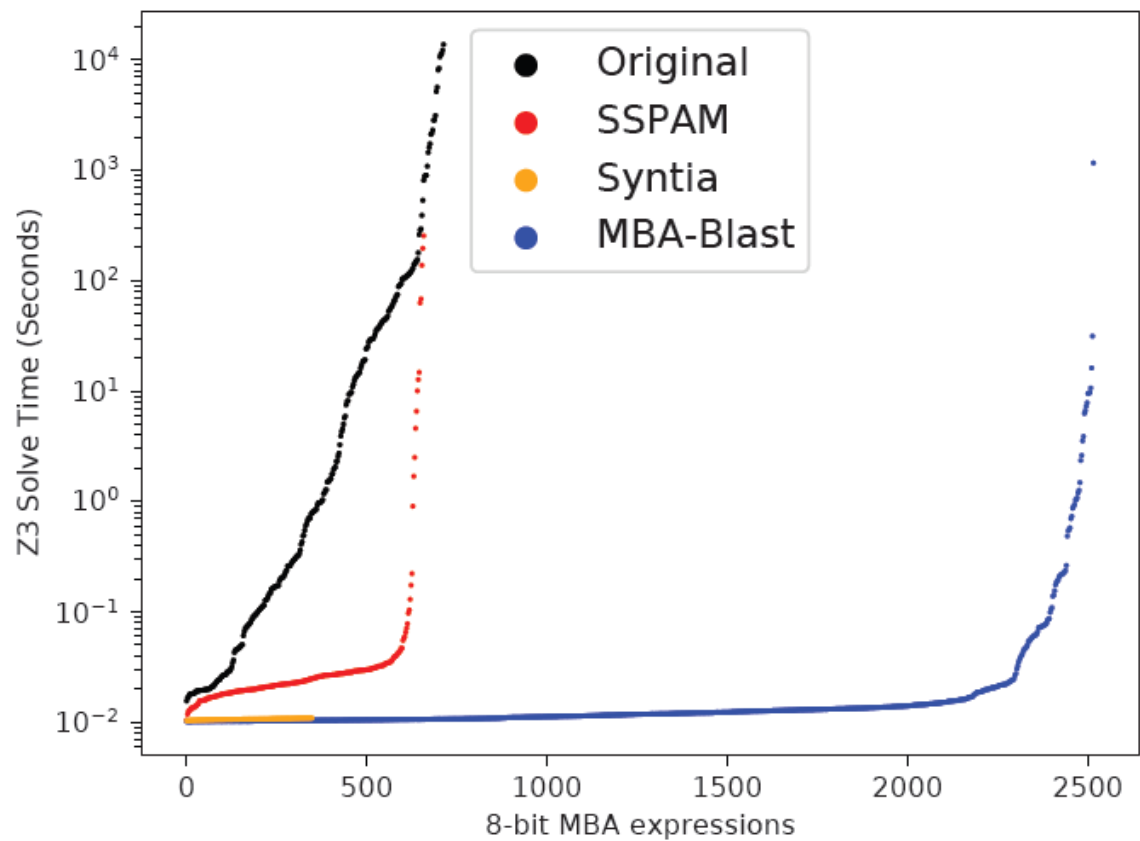
# MBA Dataset

## *Complexity Metrics*



# MBA Dataset

## *Z3 Solving Time*





# Malware Dataset

*Vmprotect*: 132 malware samples from VirusTotal

Category	Number	# with MBA	MBA Expressions
Trojan	36	30	41
Virus	33	26	40
Malware	33	26	41
Riskware	8	7	11
CoinMiner	7	6	9
Backdoor	4	2	3
ADware	4	3	4
Ransomware	3	3	5
Spyware	2	1	2
Others	2	1	1
Total	132	105	157

# Malware Dataset

*Example:*  $x - y = \sim(\sim x + y) \& \sim(\sim x + y)$

$$\sim(\sim x + y) \& \sim(\sim x + y)$$

$$= \sim t \& \sim t \quad \sim x + y \rightarrow t$$

$$= -t - 1$$

$$= -\sim x - y - 1 \quad t \rightarrow \sim x + y$$

$$= x - y$$

# Case Study

## *Ransomware Sample*

$$(K|\sim C) + (\sim K|C) - 2 * \sim(K|C) - 2 * (K\&C)$$

$$\begin{aligned} &= -C + (K\&C) - 1 + (-K + (K\&C) - 1) \\ &\quad - 2 * (-K - C + (K\&C) - 1) - 2 * (K\&C) \\ &= K + C - 2 * (K\&C) \end{aligned}$$

$$= (K \wedge C)$$

Conclusion

MBA-Blast is  
the most generic and efficient  
MBA deobfuscation technique



*Thanks!*

[Binbin.liu@unh.edu](mailto:Binbin.liu@unh.edu)

[Dongpeng.xu@unh.edu](mailto:Dongpeng.xu@unh.edu)

<https://github.com/softsec-unh/MBA-Blast>