

# Paying Less for More? Combo Plans for Edge-Computing Services

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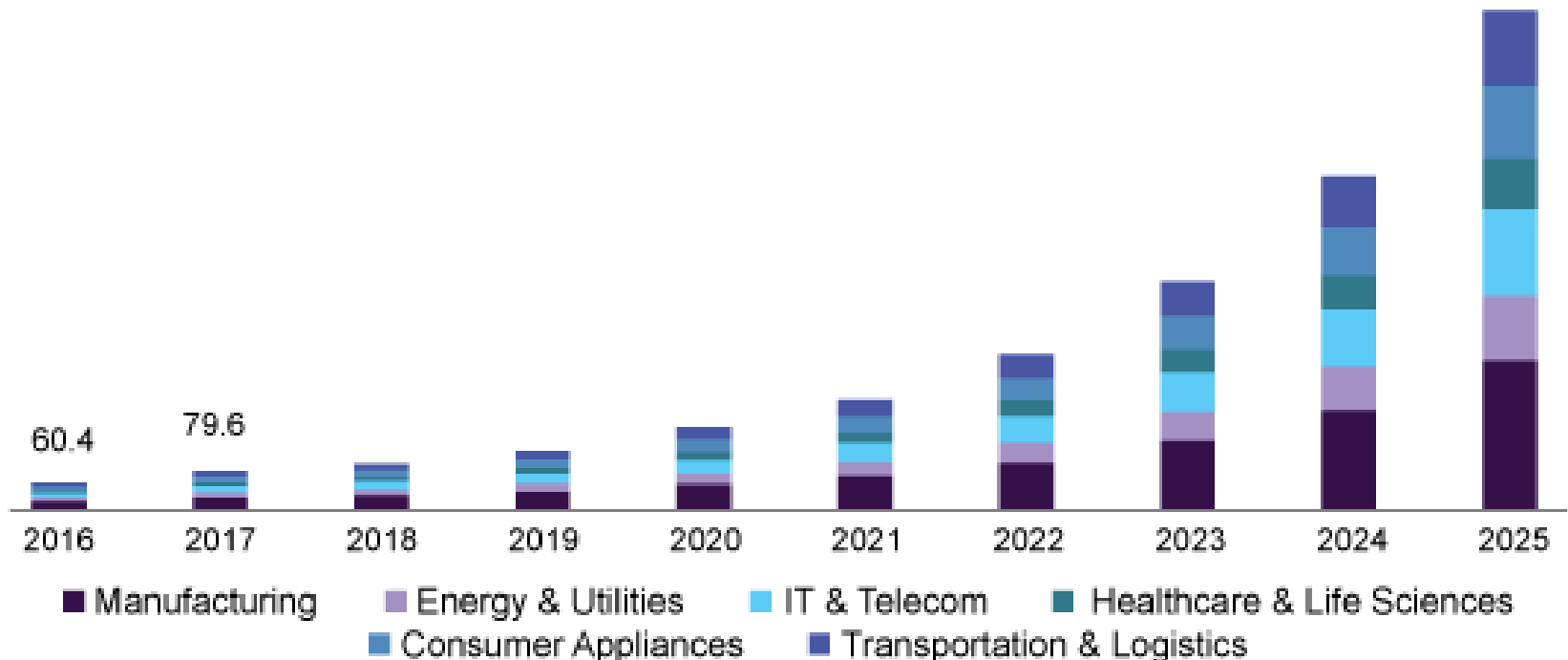


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- › Background and Motivation
- › System Model and Problem Formulation
- › Problem Solution: Smart Online Reservation Algorithm
- › Simulation Result
- › Conclusion

## Edge-computing market opportunity and potential

U.S. edge computing market, by vertical, 2016 - 2025 (USD Million)



- › Vodafone and Continental are using edge computing to make Germany's roads safer.
- › AT&T is using edge computing for smart city IoT.
- › Amazon, HPE and Saguna are building the edge-computing platforms.

- Pricing: 1. How do edge-computing service providers design the plans?  
2. How do customers reserve the plans?



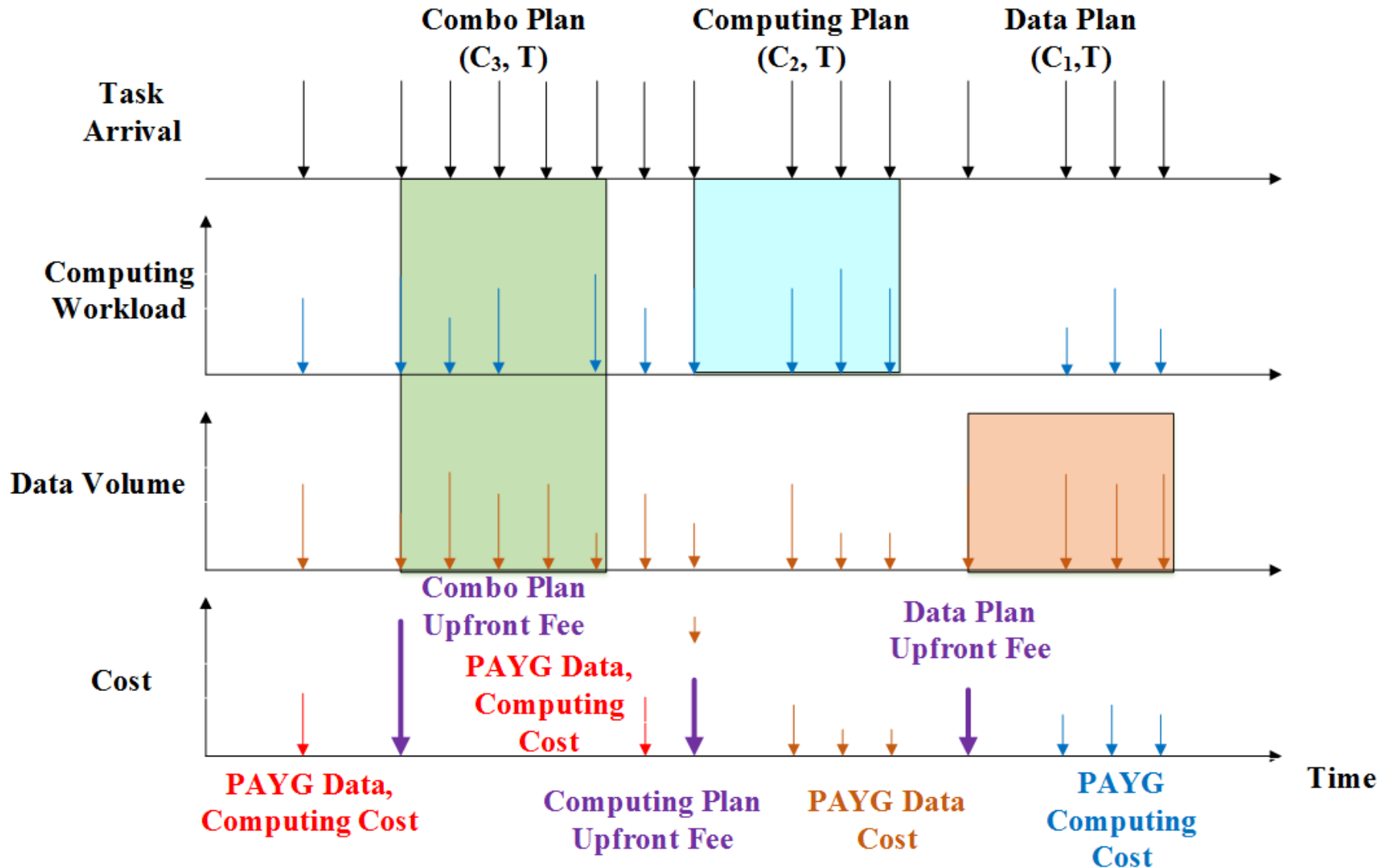
- › Individual plans for computing workload and data volume.

Computing plan (edge computing)  $\leftrightarrow$  Cloud computing plan

Data plan (edge computing)  $\leftrightarrow$  mobile phone data plan

- › Combo plan for edge-computing services covering both data volume and computing workload.

# System Model and Problem Formulation



## Comparison

- › PAYG: no long term commitment, pay for what you use.
- › Plans: high upfront fee cost, save money if many tasks come in the following reservation period.

	Flexibility	Upfront Fee	Coverage
PAYG Data	High	0	Small
Data Plan	Medium	$C_1$	Medium
Computing Plan	Medium	$C_2$	Medium
Combo Plan	Low	$C_3$	High



## Online plan reservation problem

- › To reserve not to reserve a plan? To reserve which plan?  
(cost minimization)
- › Online reservation: the future information is incomplete or unreliable.
- › Once the edge-computing service provider knows users' strategy, it can adjust the combo plan price to maximize its profit.

# System Model and Problem Formulation

Competitive ratio: measure of online algorithms

› Compare the online strategy with the optimal offline algorithm.

›  $\mathcal{S}$ : any edge-computing service request sequence

$C_A(\mathcal{S})$ : cost of online reservation algorithm  $A$

$C_{OPT}(\mathcal{S})$ : cost of optimal offline reservation algorithm

$$C_A(\mathcal{S}) \leq c \cdot C_{OPT}(\mathcal{S})$$

› An optimal online algorithm gives minimal  $c$  for all possible  $\mathcal{S}$ .

## Outline of Smart Online Reservation Algorithm

### › Input

Typical data cost: sum of PAYG data cost during  $(t - T, T]$

Typical computing cost: sum of PAYG computing cost during  $(t - T, T]$

### › Output

Plan reservation decisions for the sequence of edge-computing tasks.

{PAYG, data plan, computing plan and combo plan}

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## Algorithm 1 SOR Case 1: Inexpensive Combo Plan

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- 1: Proceed if there is a new task.
  - 2: **if** there is no on-going combo plan **then**
  - 3: | Calculate  $x$  and  $y$  as the typical data cost and computing cost.
  - 4: | **if**  $x + y \geq C_3$  **or**  $y \geq C_2$  **or**  $x \geq C_1$  **then**
  - 5: | | Reserve a combo plan.
  - 6: | **else**
  - 7: | | Satisfy the task by PAYG.
  - 8: | **end if**
  - 9: **end if**
  - 10: Repeat from step 1.
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## Working principle

- › Main idea: minimize the competitive ratio at the worst case (most adverse edge-computing service request sequence)
- › Worst case: after the algorithm reserves a plan, no corresponding request comes.

$$\min_{x,y,p} \frac{x + y + u(\mathbf{p})}{c_{opt}(x, y)}$$

Online algorithm cost  
Optimal offline cost

$x$ : typical data cost,  $y$ : typical computing cost,  $u(\mathbf{p})$ : upfront fees with plan choices  $\mathbf{p}$

## Findings

- › Competitive ratio of SOR:  $1 + \frac{C_1 + C_2}{C_3}$  (minimum among all online deterministic algorithms).
- › SOR only reserves the combo plan when
$$C_3 < \min(\sqrt{C_1(C_1 + C_2)}, \sqrt{C_2(C_1 + C_2)})$$
- › Critical price point: combo plan is more attractive compared with individual plans below this point.

## Trace Driven Performance Comparison

- › Compare the overall cost performance with the following benchmark strategies.

PAYG only (P): All tasks are satisfied by PAYG.

Combo only (C): A combo plan is purchased when a new task arrives and the previous combo plan expires.

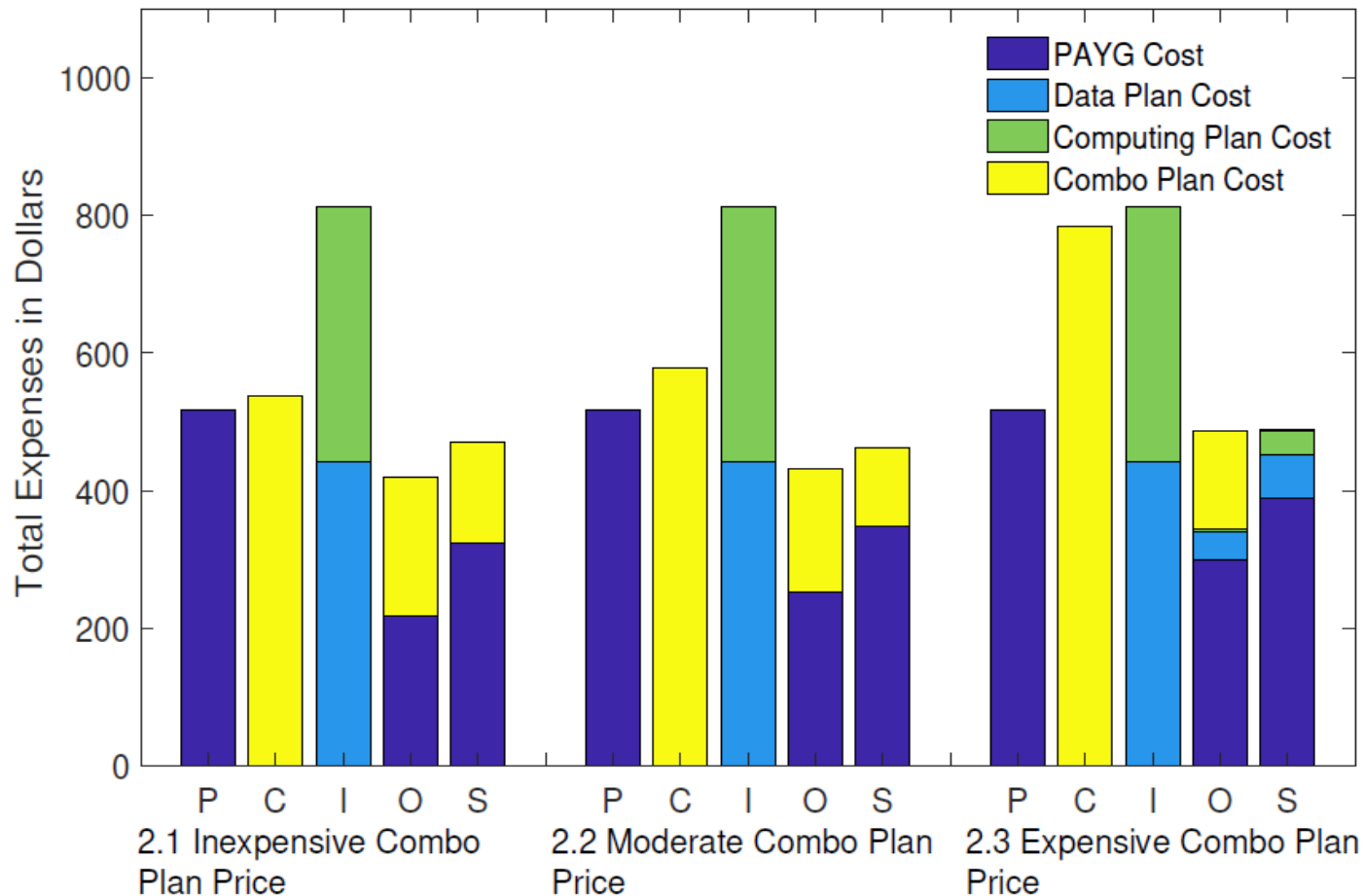
## Trace Driven Performance Comparison

Individual plan (I): A data or computing plan is purchased when new data volume or computing workload arrives and the previous plan expires.

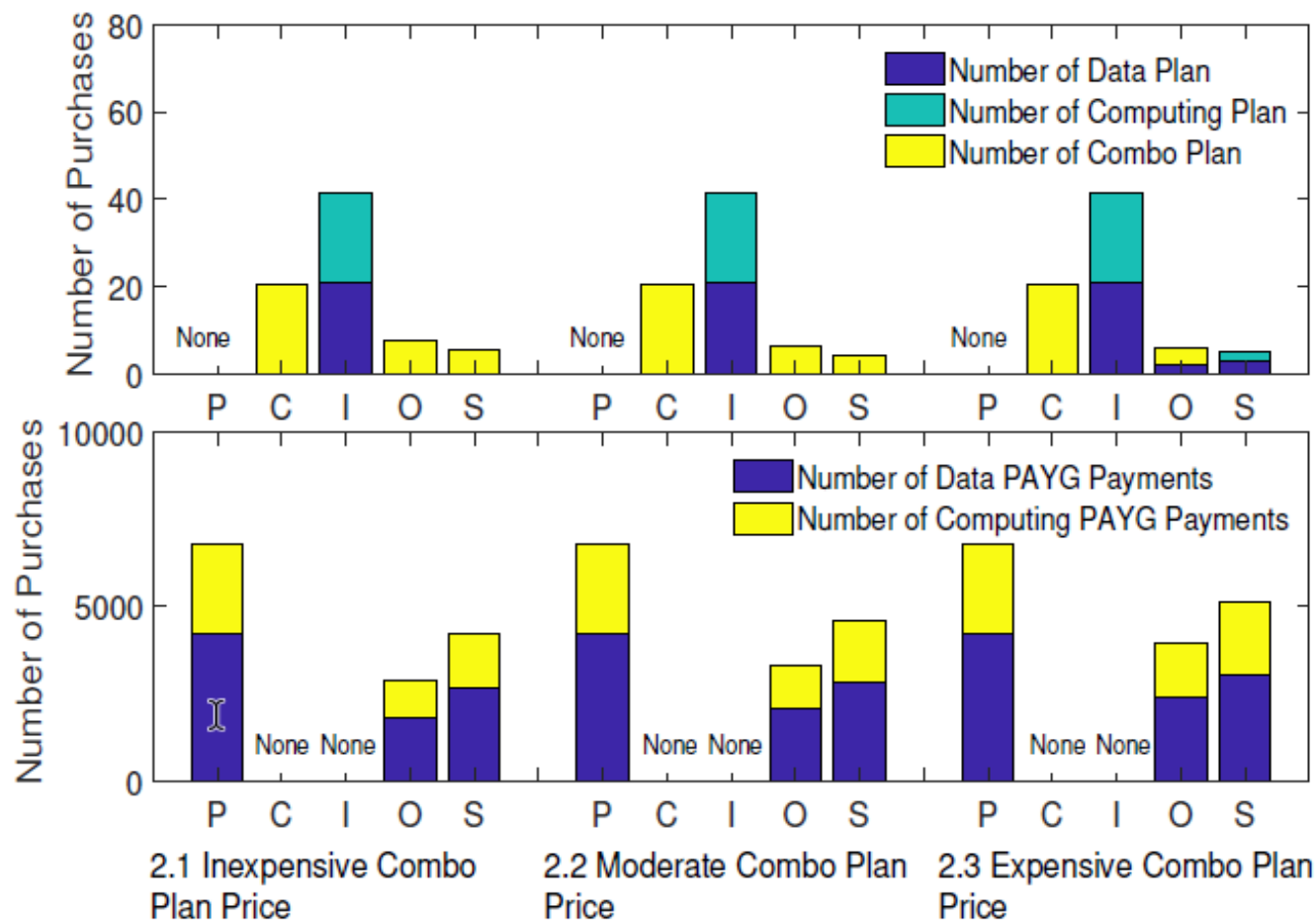
Offline (O): The user knows all task arrivals in advance and purchase a plan to make sure that the sum of further PAYG cost it will cover is greater than the plan upfront fee.



P: PAYG only, C: Combo only, I: Individual plans, O: Offline, S: Smart online reservation algorithm



P: PAYG only, C: Combo only, I: Individual Plan, O: Offline, S: Smart online reservation algorithm



- › Online plan reservation problem for edge-computing services.
- › Smart Online Reservation algorithm gives optimal competitive ratio among all deterministic algorithms.
- › Critical price point: combo plan is more attractive compared with individual plans below this point.
- › Feedback: combo plan about the edge computing

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## PAYG and Individual Plans

- › PAYG (data) : satisfy required data volume  $a$  with unit data price  $p_1$  and the cost is  $a \times p_1$ .
- › PAYG (computing) : satisfy required computing workload  $b$  with unit computing price  $p_2$  and the cost is  $b \times p_2$
- › Data plan: cover all the data volume in the following reservation period  $T$  with upfront fee  $C_1$
- › Computing plan: cover all the computing workload in the following reservation period  $T$  with upfront fee  $C_2$ .

## Combo Plan

- › Combo plan: cover all the data volume and computing workload in the following reservation period  $T$  with upfront fee  $C_3$ .
- › Combo plan price  $C_3$  :  $C_3 > C_1$  (data plan price),  $C_3 > C_2$  (computing plan price),  $C_3 \leq C_1 + C_2$ .